

报告名称: MSR codes with linear field size and smallest sub-packetization for any number of helper nodes

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报告摘要: The sub-packetization  $\ell$  and the field size  $q$  are of paramount importance in the MSR array code constructions. For optimal-access MSR codes, Balaji et al. proved that  $\ell \geq s^{\lceil n/s \rceil}$ , where  $s = d-k+1$ . Rawat et al. showed that this lower bound is attainable for all admissible values of  $d$  when the field size is exponential in  $n$ . After that, tremendous efforts have been devoted to reducing the field size. However, till now, reduction to linear field size is only available for  $d \in \{k+1, k+2, k+3\}$  and  $d=n-1$ .

In this work, we construct the first class of explicit optimal-access MSR codes with the smallest sub-packetization  $\ell = s^{\lceil n/s \rceil}$  for all  $d$  between  $k+1$  and  $n-1$ , resolving an open problem in the survey (Ramkumar et al., Foundations and Trends in Communications and Information Theory: Vol. 19: No. 4). We further propose another class of explicit MSR code constructions (not optimal-access) with even smaller sub-packetization  $s^{\lceil n/(s+1) \rceil}$  for all admissible values of  $d$ , making significant progress on another open problem in the survey. Previously, MSR codes with  $\ell = s^{\lceil n/(s+1) \rceil}$  and  $q = O(n)$  were only known for  $d=k+1$  and  $d=n-1$ . The key insight that enables a linear field size in our construction is to reduce  $\binom{n}{r}$  global constraints of non-vanishing determinants to  $O_s(n)$  local ones, which is achieved by carefully

designing the parity check matrices. This is a joint work with Guodong Li, Ningning Wang, and Min Ye.